



*3d curvilinear skeletonization algorithm  
with application to path tracing*



*a story by*

*John Chaussard - Laurent Noël  
Venceslas Biri - Michel Couprie*

*produced by*





ONCE UPON  
A TIME..



ONCE UPON  
A TIME..





ONCE UPON  
A TIME..





ONCE UPON  
A TIME!





ONCE UPON  
A TIME..





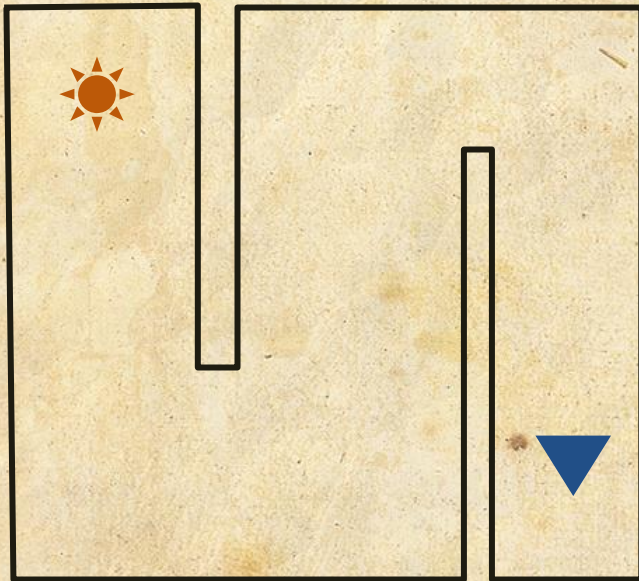
# Path-tracing

Path-tracing is an algorithm to create **photo realistic images** from a scene.



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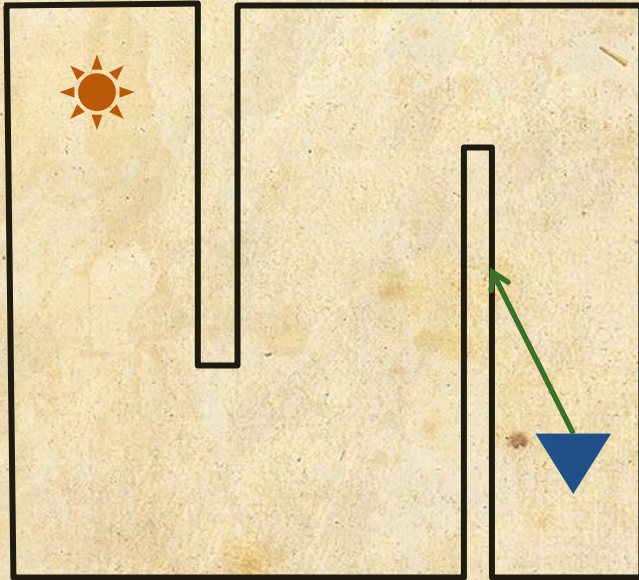
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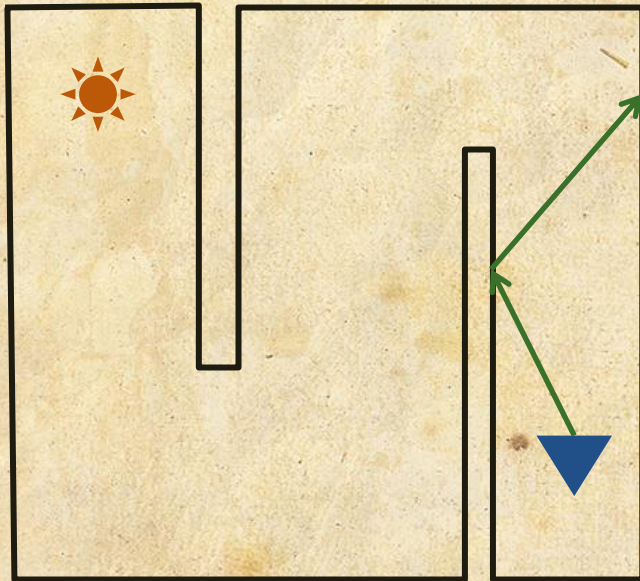


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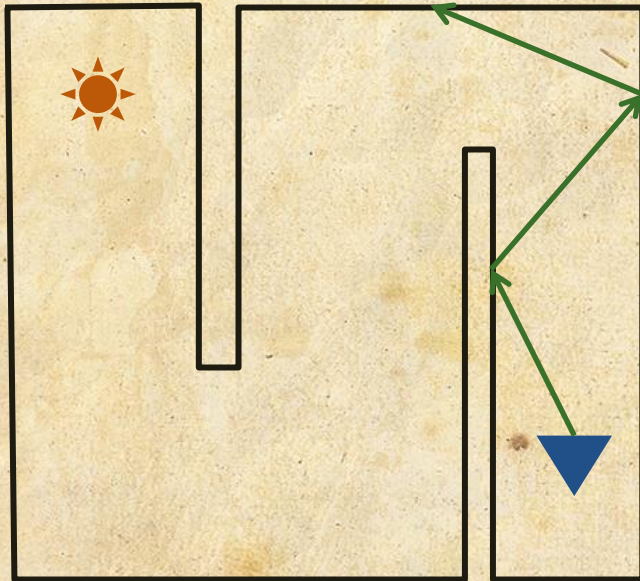
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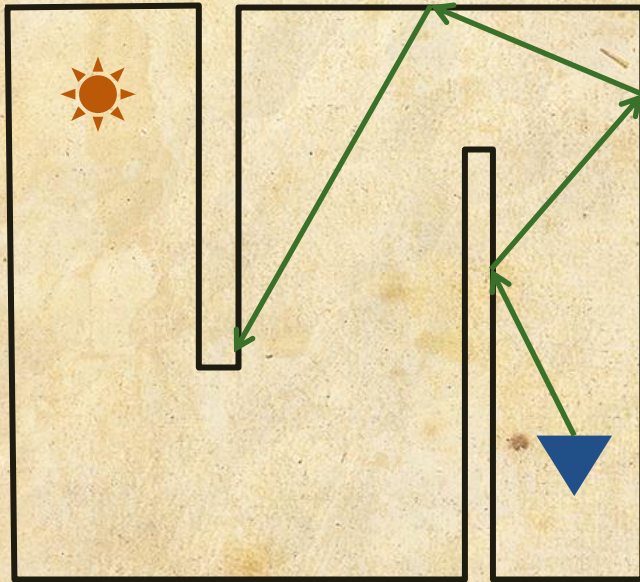
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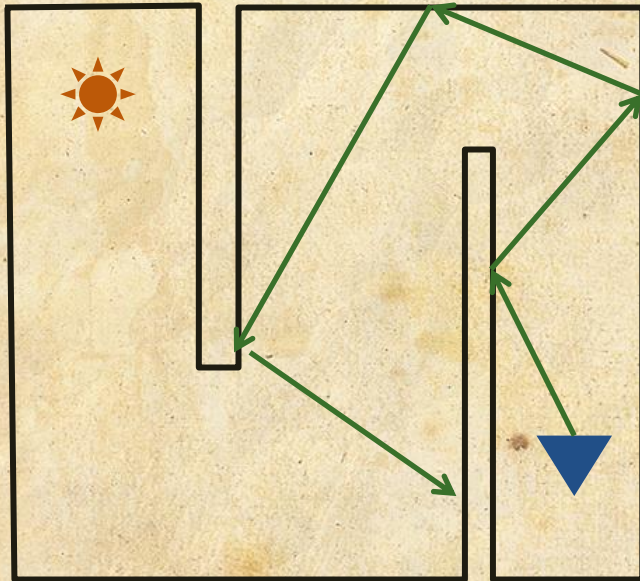
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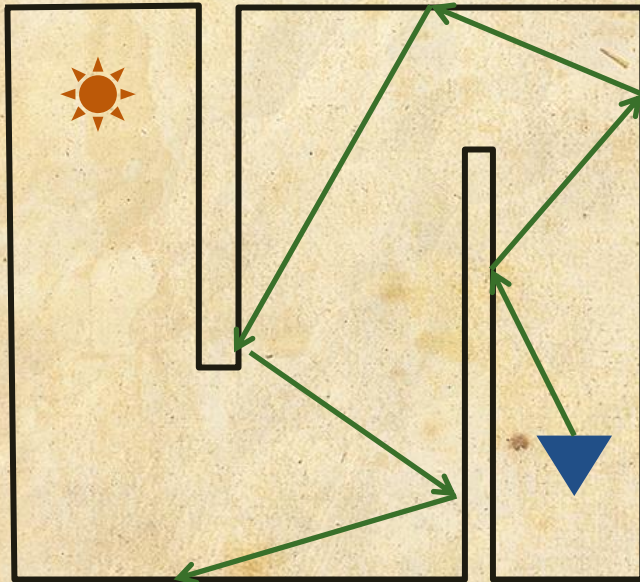
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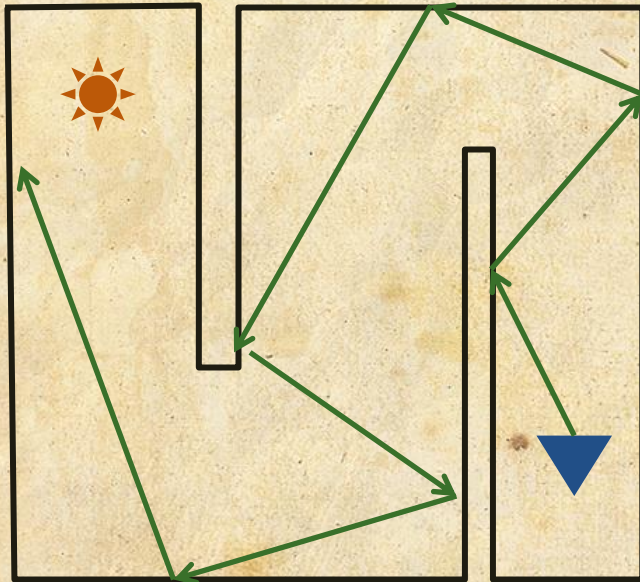
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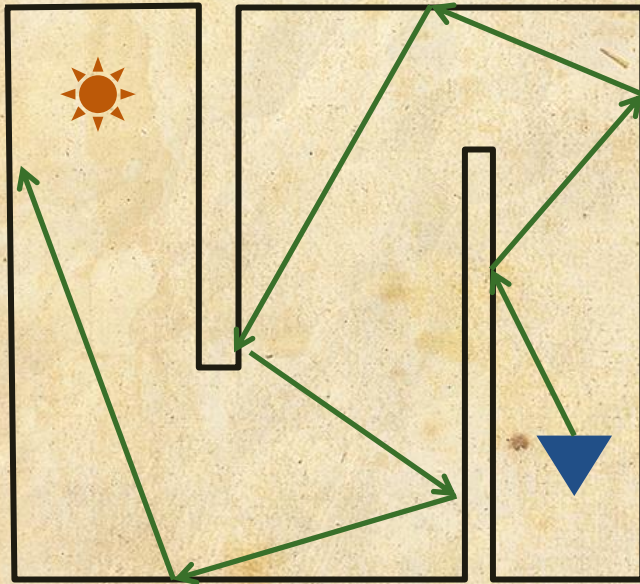
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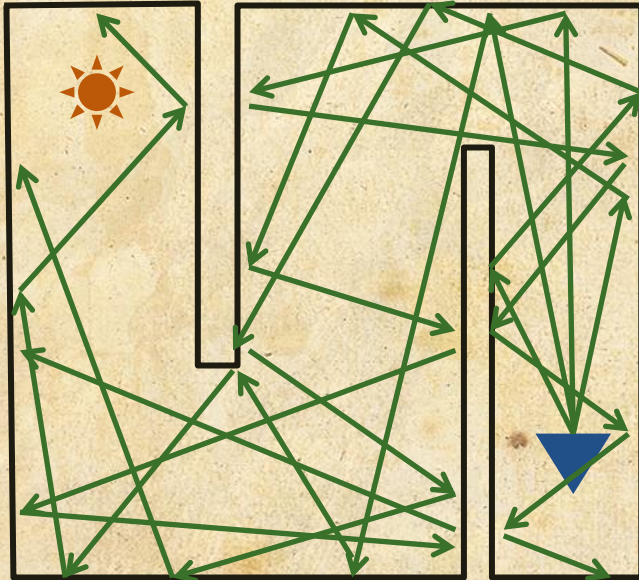
The BRDF function of an object tells how light tends to reflect on this object.

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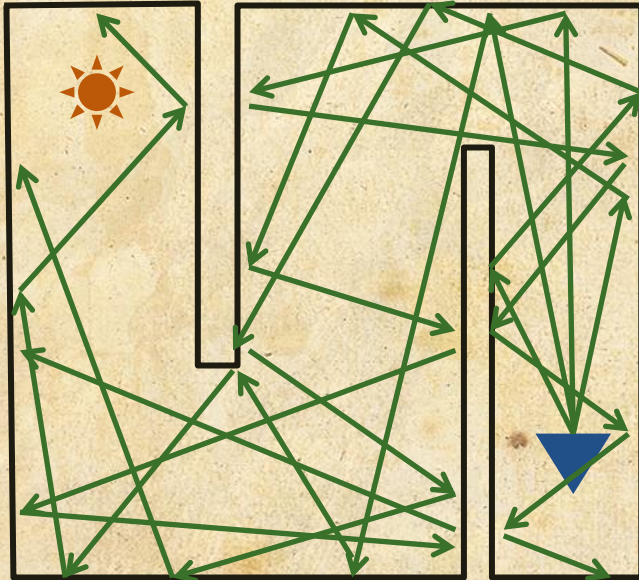
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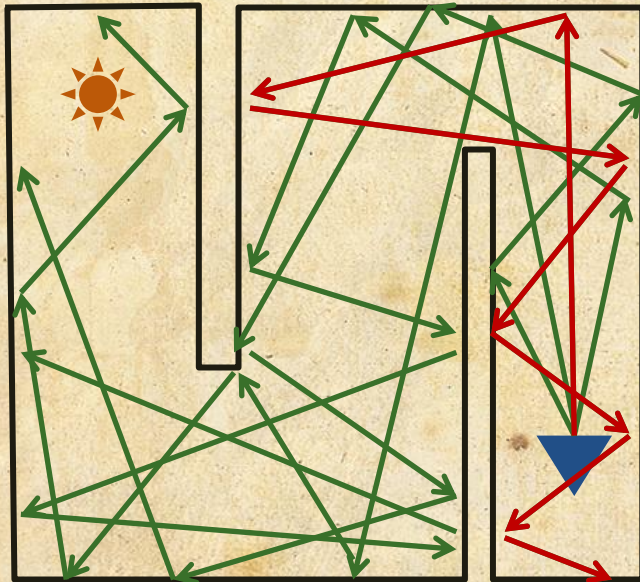


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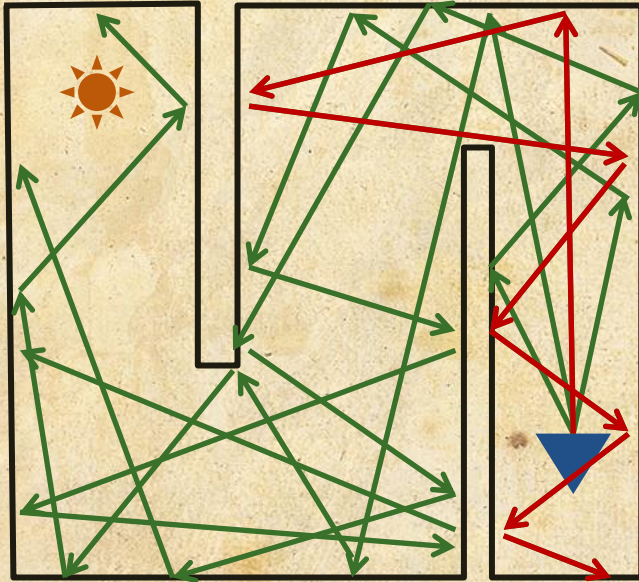
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Some rays never reach any bright area of the scene : these rays collect little information on the scene and don't contribute much to the final result.



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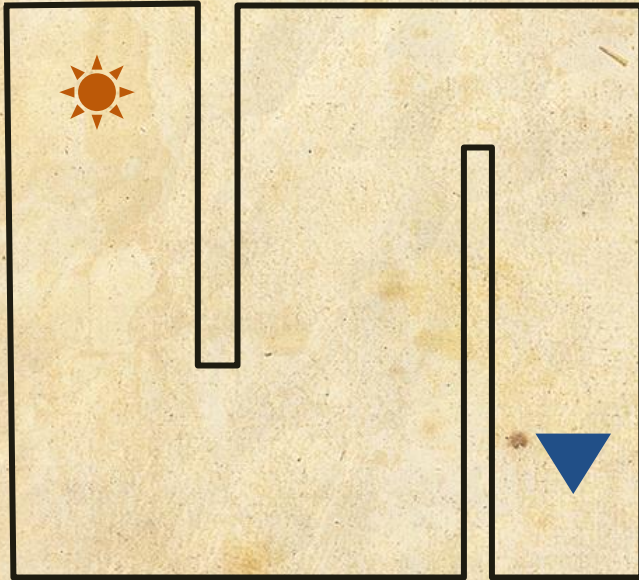
Some rays never reach any bright area of the scene : these rays collect little information on the scene and don't contribute much to the final result.

Reducing the number of these non contributing rays is a way to make the computation faster without changing the output quality.



# Path-tracing

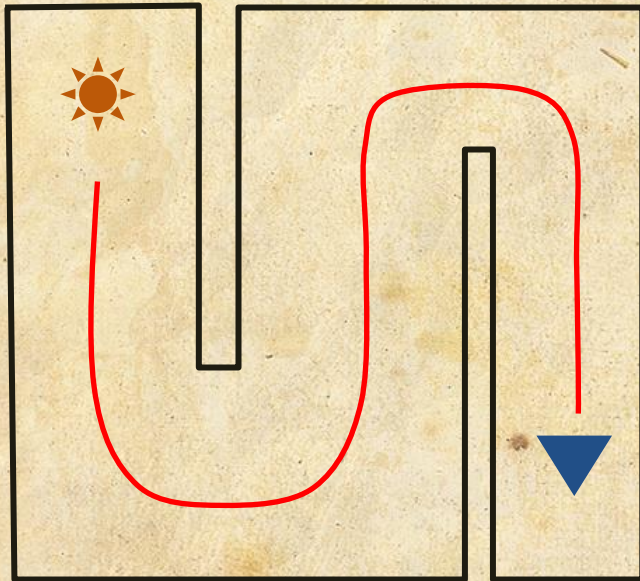
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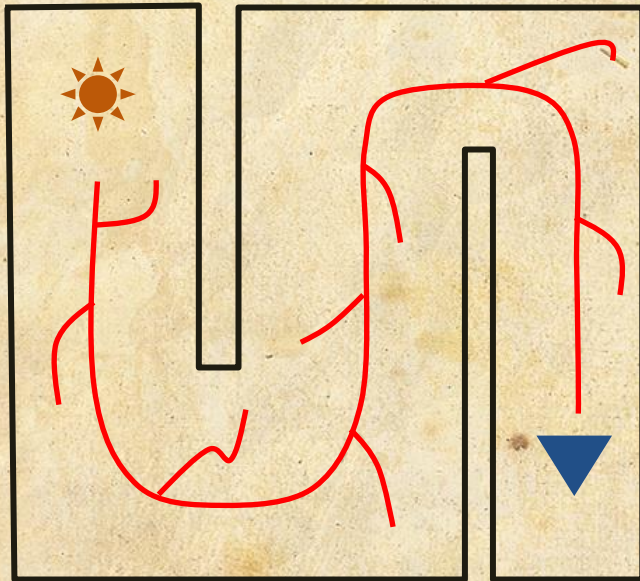


We hope that this strategy will help reduce the number of non contributing rays and will **make the computation faster**.



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Our idea is to use a **skeleton of the voids of the scene** in order to **guide the rays towards the bright areas** of the scene.



We hope that this strategy will help reduce the number of non contributing rays and will **make the computation faster**.

To be efficient, we need a **skeleton which « looks » like the original object** and **contain as few spurious branches as possible**.

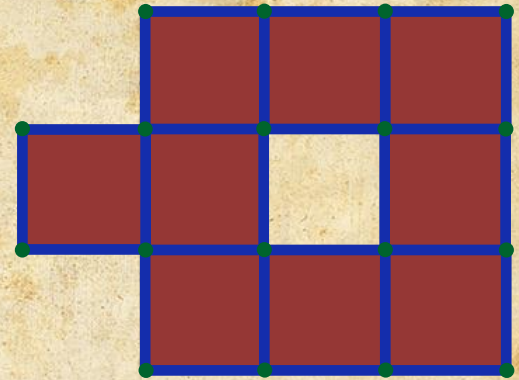


# Curvilinear skeletonization algorithm



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Our skeletonization algorithm works on **cubical complexes framework**: objects are not made of voxels, but of cubes, squares, lines and points (called faces).

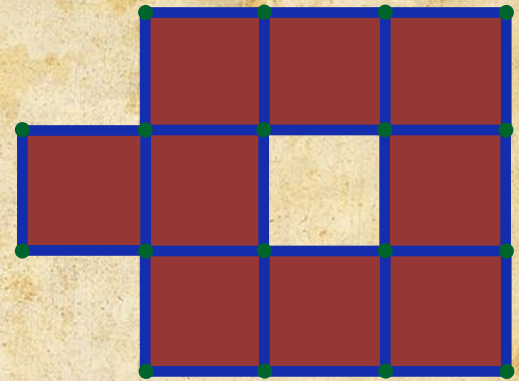




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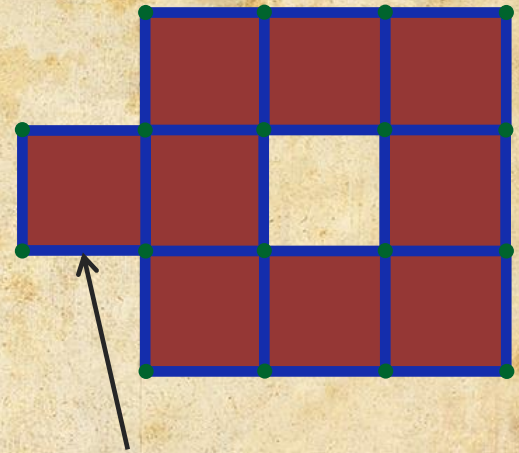




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*This line touches exactly one square : it is free*

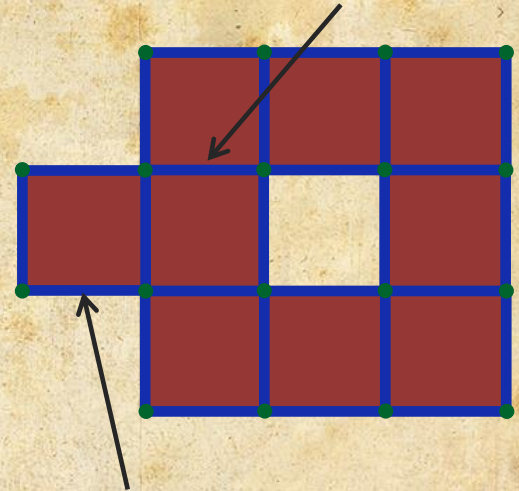


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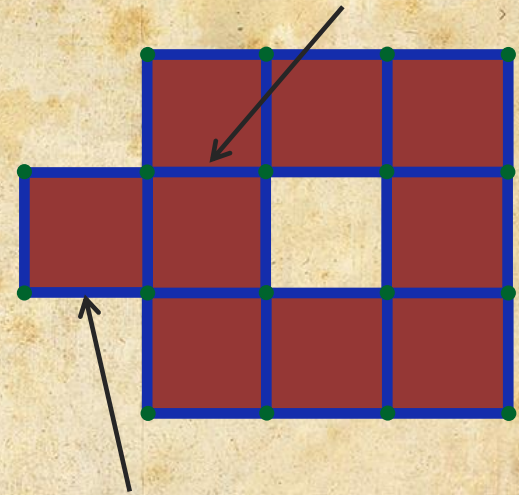
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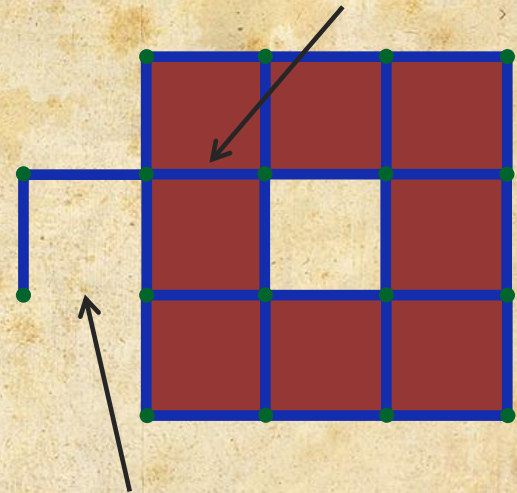
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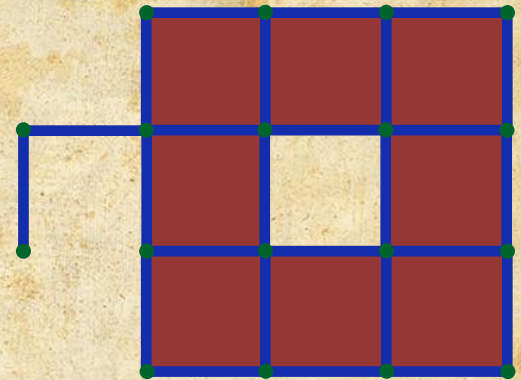


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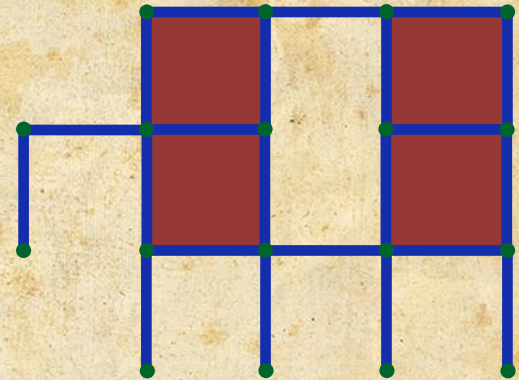


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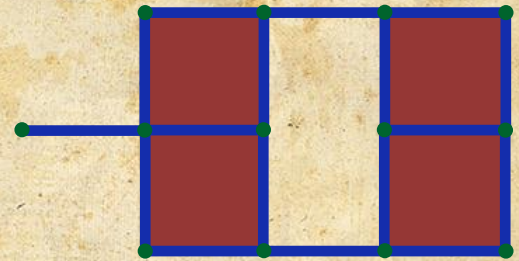


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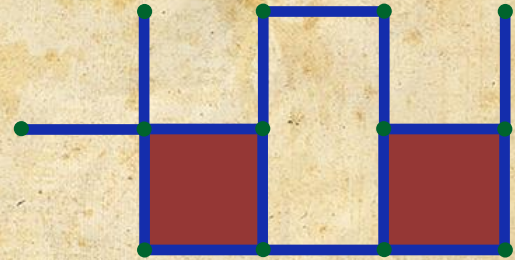


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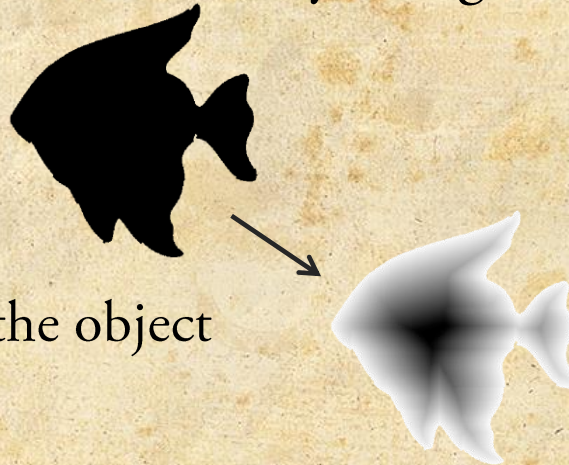
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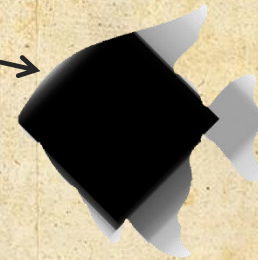
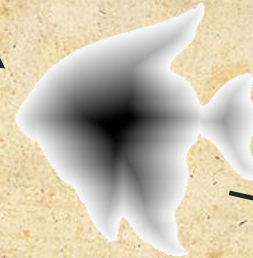


The 6-distance map of the object



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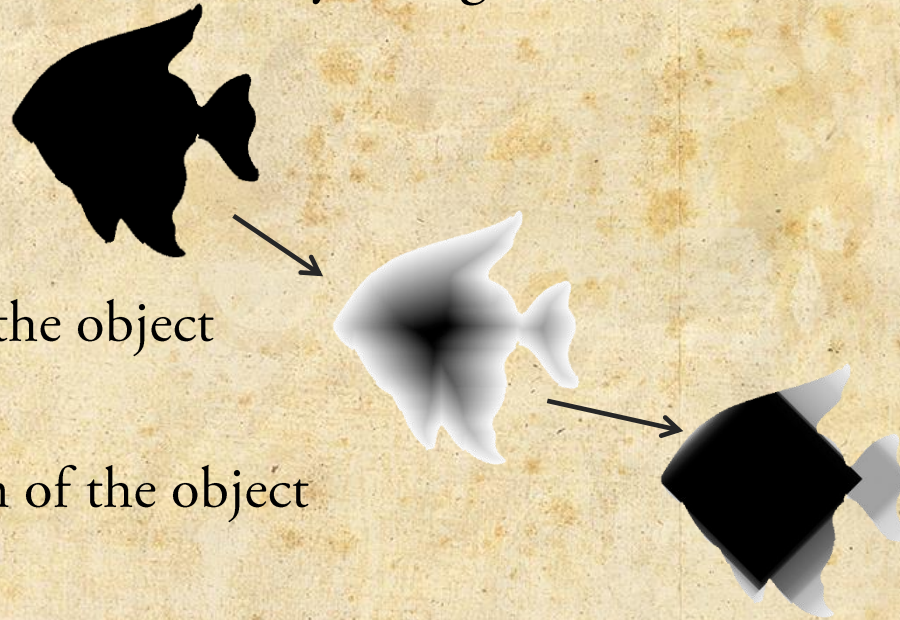
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The 6-opening function of the object



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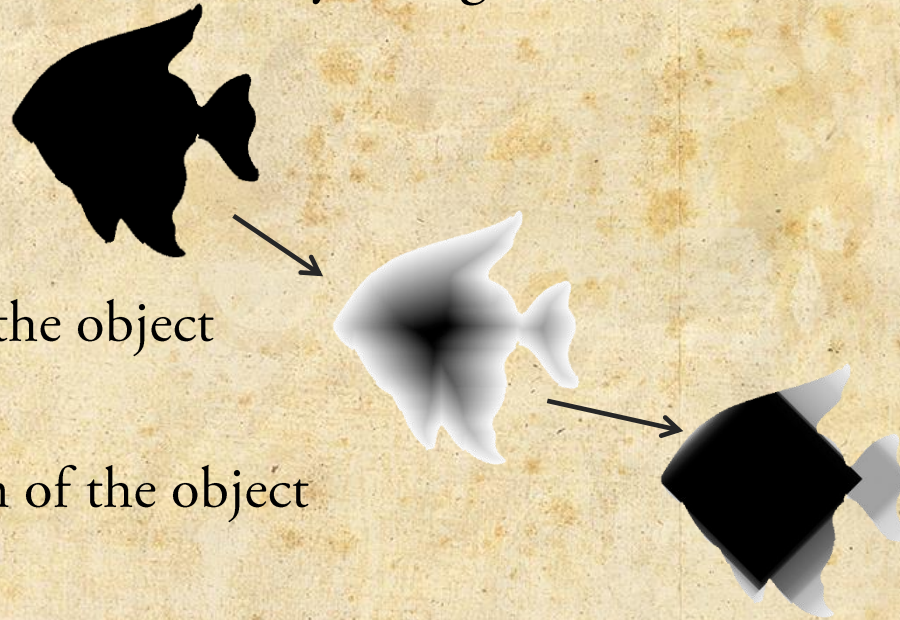
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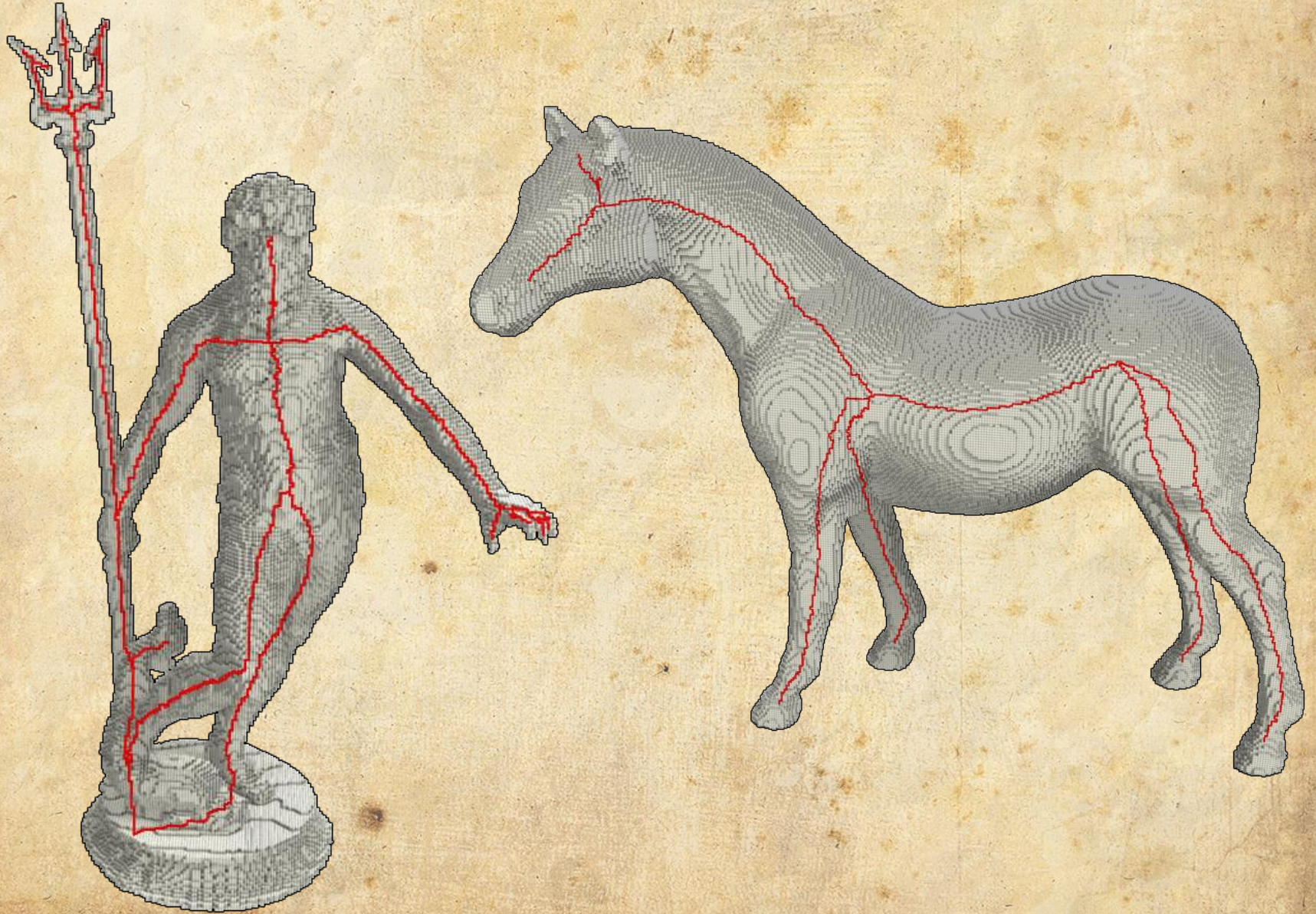
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**The algorithm is entirely automatic:** it does not need any user input to perform the filtering.



# Curvilinear skeletonization algorithm





# Skeleton path-tracing

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**These two elements must be carefully averaged** in order to still obtain photorealistic images and reduce the number of non contributing rays.



# Skeleton path-tracing

## Workflow

```
DEF arcs_floor_small Transform {
  translation 0.00724 0.09331 0.00149
  rotation -1 0 0 -1.571
  children [
  Shape {
    appearance Appearance {
      material Material {
        diffuseColor 0.7451 0.7098 0.6745
        ambientIntensity 0
        specularColor 0 0 0
        shininess 0.525
        transparency 0
      }
      texture ImageTexture {
        url "../maps/sp_luk.JPG"
      }
    }
  }
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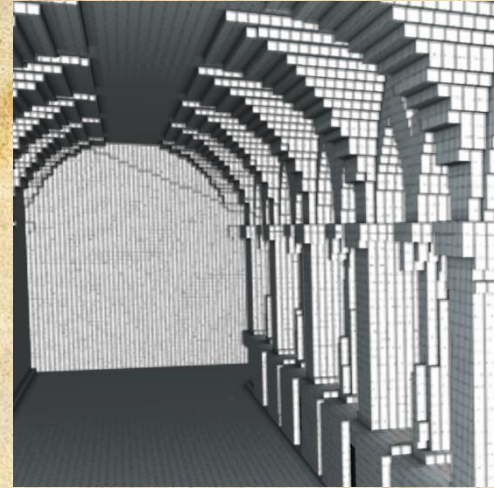


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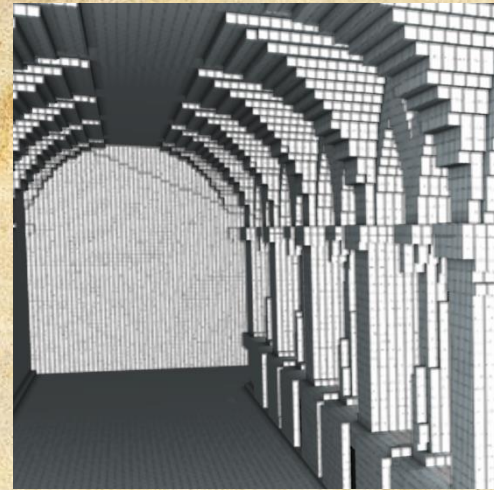


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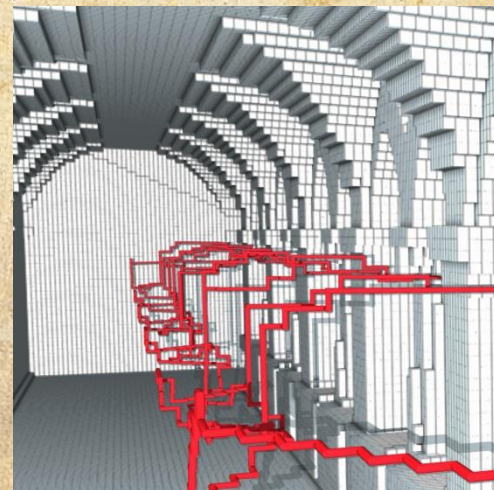
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→  
*voxelization*



↓  
*thinning*



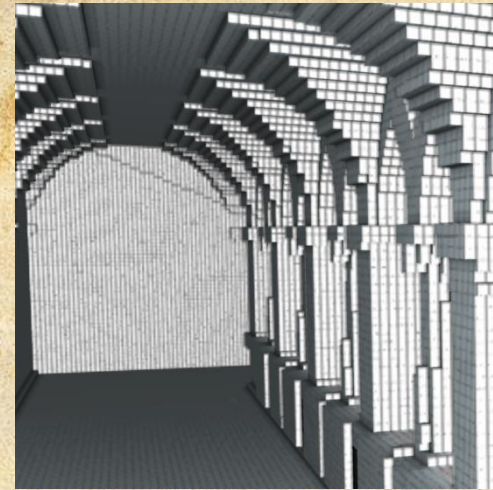


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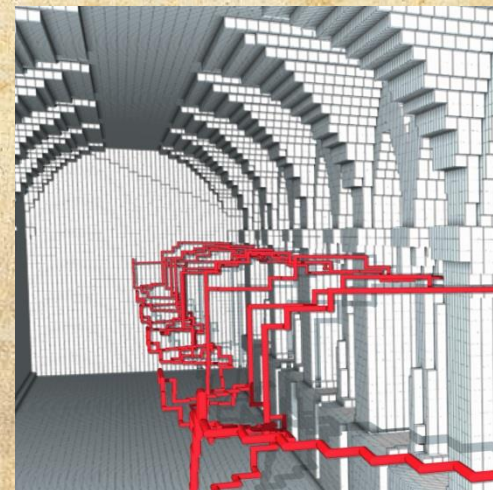
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←  
*skeleton  
path-tracing*

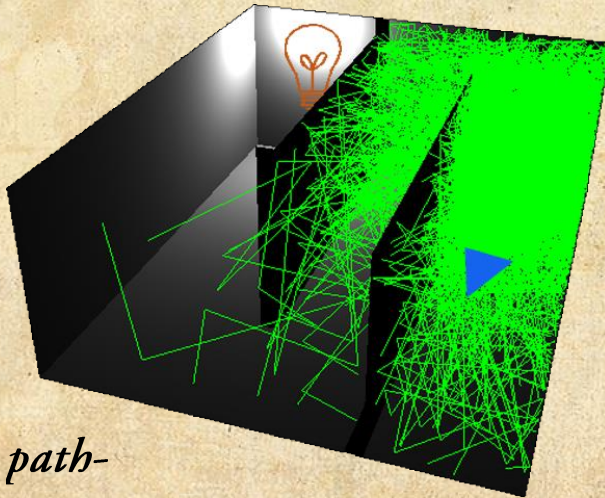




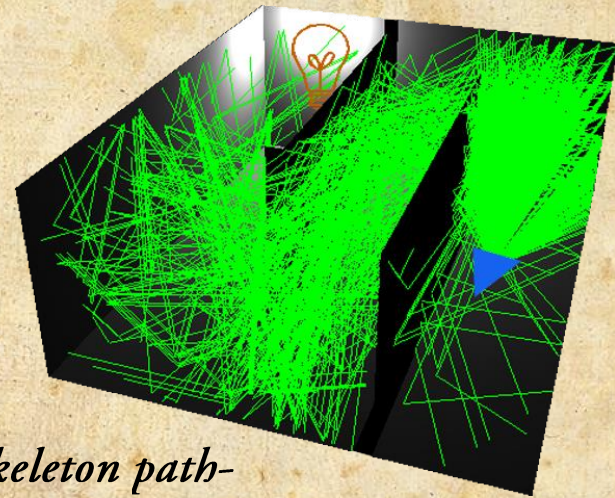
# Skeleton path-tracing

## Results:

For a same amount of rays sent in the scene, **our method produces more rays reaching bright areas** (useful rays).



*classical path-  
tracing*



*skeleton path-  
tracing*

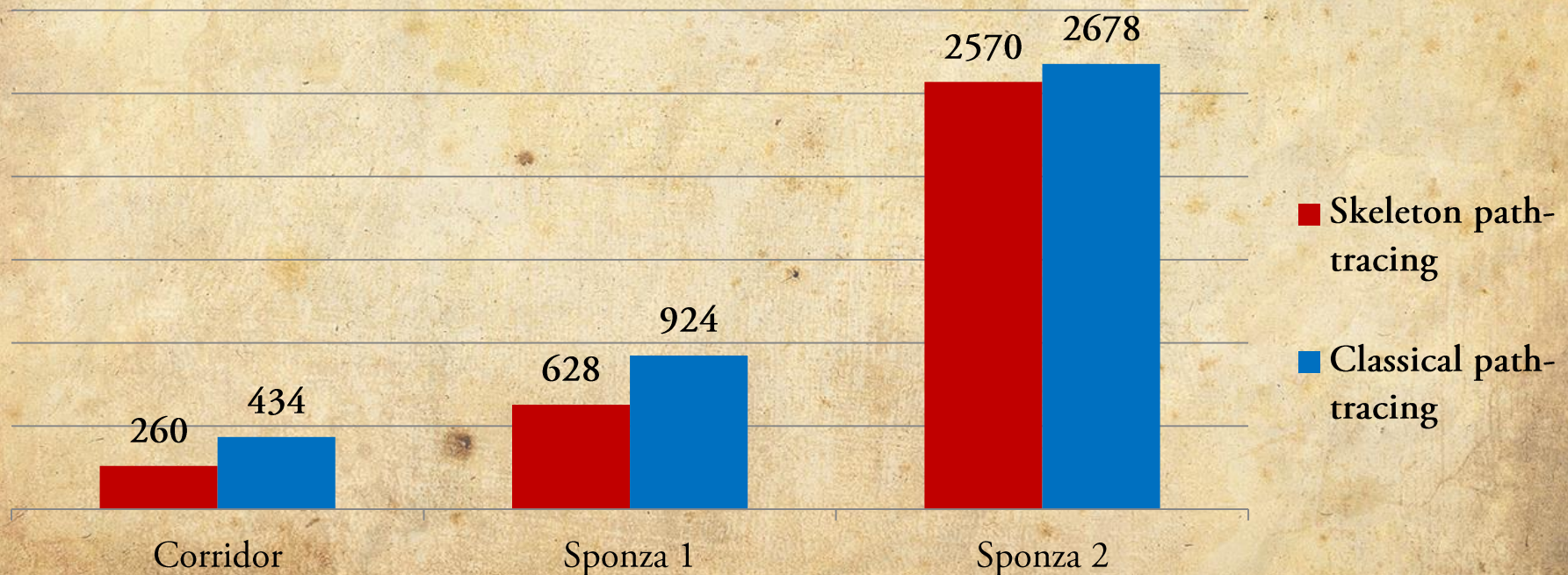


# Skeleton path-tracing

## Results:

**Our method is faster** than classical path-tracing to produce same quality images.

Computation time (in sec.) to obtain an image with an MSE of 40 against ground truth

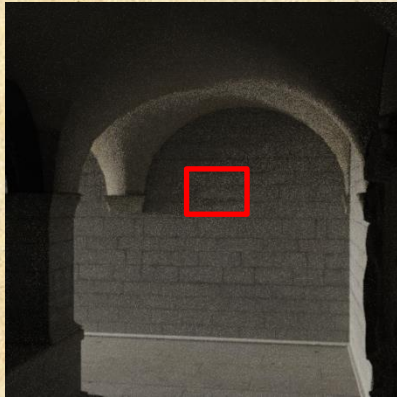




# Skeleton path-tracing

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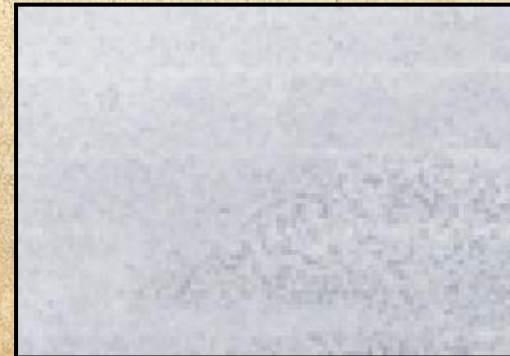
Our method produces less noisy images.



*classical path-tracing*



*skeleton path-tracing*





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